

- Previous 11 Years Chapter-wise Questions
- Hints & Explanations for all Questions
- Last 6 years question paper trend analysis
- Authentic Paper
   Errorless Solution



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A-23 FIEE Complex, Okhla Phase II New Delhi-110020 Tel: 49842349/ 49842350

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## **Free Sample Contents**

#### PHYSICS

3. Motion in a Plane

#### MATHEMATICS

12. Limits and Derivatives

This sample book is prepared from the book "Latest New Syllabus 11 Chapter-wise Karnataka CET Physics, Chemistry & Mathematics Previous Year Solved Papers (2024 - 2014) 2nd Edition | KCET PYQs Question Bank | 2025 Engineering B.Tech/ BE & B.Sc.".

2nd Edition



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	•		- - - - - -		



### **Motion in a Plane**

1. Among the given pair of vectors, the resultant of two vectors can never be 3 units. The vectors are

[2024]

7.

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- (a) 1 unit and 2 units (b) 2 units and 5 units
- (c) 3 units and 6 units (d) 4 units and 8 units
- 2. A particle is in uniform circular motion. Related to one complete revolution of the particle, which among the statements is incorrect? [2023]
  - (a) Displacement of the particle is zero.
  - (b) Average speed of the particle is zero.
  - (c) Average velocity of the particle is zero.
  - (d) Average acceleration of particle is zero.
- 3. Two objects are projected at an angle  $\theta^{\circ}$  and  $(90 \theta)^{\circ}$ , to the horizontal with the same speed. The ratio of their maximum vertical heights is [2022]
  - (a)  $1: \tan \theta$  (b) 1: 1
  - (c)  $\tan^2 \theta$ : 1 (d)  $\tan \theta$ : 1
- 4. The maximum range of a gun on horizontal plane is 16 km. If g = 10 m s<sup>-2</sup>, then muzzle velocity of a shell is [2021]
  - (a)  $160 \text{ m s}^{-1}$  (b)  $200 \sqrt{2} \text{ m s}^{-1}$
  - (c)  $400 \text{ m s}^{-1}$  (d)  $800 \text{ m s}^{-1}$
- 5. The trajectory of a projectile is [2021]
  - (a) semicircle
  - (b) an ellipse
  - (c) a parabola always
  - (d) a parabola in the absence of air resistance.
- 6. For a projectile motion, the angle between the velocity and acceleration is minimum and acute at [2021]
  - (a) only one point (b) two points
  - (c) three points (d) four points

A particle starts from the origin at t = 0 s with a velocity of  $10\hat{j}$  m s<sup>-1</sup> and moves in the x - y plane with a constant acceleration of  $(8\hat{i} + 2\hat{j})$  m s<sup>-2</sup>. At an instant when the *x*-coordinate of the particle is 16 m, *y*-coordinate of the particle is **[2021]** (a) 16 m (b) 28 m (c) 36 m (d) 24 m

- 8. Rain is falling vertically with a speed of  $12 \text{ m s}^{-1}$ . A woman rides a bicycle with a speed of  $12 \text{ m s}^{-1}$  in east to west direction. What is the direction in which she should hold her umbrella? [2020]
  - (a) 30° towards West
  - (b) 45° towards West
  - (c) 30° towards East
  - (d) 45° towards East
  - A wheel starting from rest gains an angular velocity of 10 rad  $s^{-1}$  after uniformly accelerated for 5 sec. The total angle through which it has turned is

[2020]

- (a) 25π rad
- (b)  $50\pi$  rad about a vertical axis
- (c) 25 rad
- (d) 100 rad

10. The trajectory of a projectile projected from origin is

given by the equation  $y = x - \frac{2x^2}{5}$ . The initial velocity of the projectile is [2019]

- (a)  $25 \text{ m s}^{-1}$  (b)  $\frac{2}{5} \text{ m s}^{-1}$
- (c)  $\frac{5}{2}$  m s<sup>-1</sup> (d) 5 m s<sup>-1</sup>

#### **Motion in a Plane**

11. If 
$$\vec{A} = 2\hat{i} + 3\hat{j} + 8\hat{k}$$
 is perpendicular to  
 $\vec{B} = 4\hat{j} - 4\hat{i} + \alpha\hat{k}$ , then the value of '\alpha' is [2017]

(a) 1 (b)  $\frac{1}{2}$  (c) -1 (d)  $-\frac{1}{2}$ 

**12.** The angle between velocity and acceleration of a particle describing uniform circular motion is

[2017]

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- (a)  $180^{\circ}$  (b)  $45^{\circ}$  (c)  $90^{\circ}$  (d)  $60^{\circ}$
- **13.** Three projectiles A, B and C are projected at an angle of 30°, 45°, 60° respectively. If  $R_A$ ,  $R_B$  and  $R_C$  are ranges of A, B and C respectively then (velocity of projection is same for A, B and C) [2016]
  - (a)  $R_A = R_B = R_C$  (b)  $R_A = R_C > R_B$ (c)  $R_A < R_B < R_C$  (d)  $R_A = R_C < R_B$
- 14. The component of a vector  $\vec{r}$  along *x*-axis will have a maximum value if [2016]
  - (a)  $\vec{r}$  is along +ve *x*-axis
  - (b)  $\vec{r}$  is along +ve y-axis
  - (c)  $\vec{r}$  is along –ve y–axis
  - (d)  $\vec{r}$  makes an angle of 45° with the *x*-axis

 A particle is projected with a velocity v so that its horizontal range twice the greatest height attained. The horizontal range is [2015]

(a) 
$$\frac{2v^2}{3g}$$
 (b)  $\frac{v^2}{2g}$  (c)  $\frac{v^2}{g}$  (d)  $\frac{4v^2}{5g}$ 

- 16. The ratio of angular speed of a second-hand to the hour-hand of a watch is [2015]
  (a) 60:1
  (b) 72:1
  (c) 720:1
  (d) 3600:1
- 17. Which of the following is not a vector quantity?[2014]
  - (a) Momentum (b) Weight
  - (c) Potential energy (d) Nuclear spin
- **18.** A stone is thrown vertically at a speed of 30 m s<sup>-1</sup> making an angle of  $45^{\circ}$  with the horizontal. What is the maximum height reached by the stone? Take g = 10 m s<sup>-2</sup>. [2014]
  - (a) 15 m (b) 30 m (c) 10 m (d) 22.5 m

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1	(d)	2	(b)	3	(c)	4	(c)	5	(d)	6	(a)	7	(d)	8	(d)	9	(c)	10	(d)
11	(d)	12	(c)	13	(d)	14	(a)	15	(c)	16	(c)	17	(c)	18	(d)				



#### **Motion in a Plane**

8.

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- 1. (d) The resultant of two vectors  $\vec{A}$  and  $\vec{B}$  is given by  $R_{\min} \le R \le R_{\max}$   $\Rightarrow (A-B) \le R \le (A+B)$ 
  - For A = 8 units, B = 4 units  $4 \le R \le 12$
- 2. (b) The average acceleration will be zero. Since in one complete round the displacement is zero which implies that average velocity is also zero.

3. (c) Maximum height, H = 
$$\frac{u^2 \sin^2 \theta}{2g}$$

$$H_{1} = \frac{u^{2} \sin^{2} \theta}{2g} \qquad \dots (i)$$
$$H_{2} = \frac{u^{2} \sin^{2}(90^{\circ} - \theta)}{2g} = \frac{u^{2} \cos^{2} \theta}{2g} \qquad \dots (ii)$$

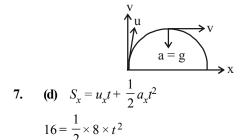
Dividing (i) by (ii), we get  $\frac{H_1}{H_2} = \frac{\tan^2 \theta}{1}$ 

4. (c) Horizontal range is maximum at  $\theta = 45^{\circ}$  $R_{\text{max}} = \frac{u^2 \sin 2\theta}{u^2 \sin 2\theta} = \frac{u^2 \sin 90^{\circ}}{u^2} = \frac{u^2}{u^2}$ 

$$g \qquad g \qquad g$$
$$\Rightarrow u = \sqrt{R_{\text{max}}g} = \sqrt{16 \times 1000 \times 10} = 400 \text{ m/s}^{-1}$$

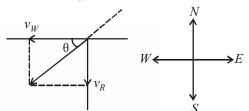
- 5. (d) In the absence of air the path of the projectile is parbolic.
- 6. (a) The acceleration due to gravity acts downwards. At maximum height velocity and acceleration is perpendicular to each other.

Thus angle will be acute for whole second half of the projectile motion but will be minimum and acute only at one point where the projectile just strikes the ground.



$$t = 2 \text{ sec.}$$

$$S_y = u_y t + \frac{1}{2} a_y t^2$$
Substitute  $t = 2$ .
$$\Rightarrow \quad 10 \times 2 + \frac{1}{2} \times 2 \times (2)^2 = 24 \text{ m}$$
(d) 
$$\tan \theta = \frac{v_R}{v_W} = \frac{12}{12} = 1 \Rightarrow \theta = \tan^{-1}(1) = 45^\circ$$



Hence, the woman should hold her umbrella 45° towards east.

(c) From equation 
$$\omega = \omega_0 + \alpha t$$
  
or  $\omega = \alpha t \Rightarrow \alpha = \frac{\omega}{t} = \frac{10}{5} = 2 \text{ rad s}^{-2}$ 

Now, using displacement,  $\theta = \omega_0 t + \frac{1}{2} \alpha t^2$ 

$$\theta = \frac{1}{2} \times 2 \times (5)^2 = 25 \, \text{rad}$$

10. (d) Standard equation,

 $y = x \tan \theta - \frac{1}{2}g \frac{x^2}{u^2 \cos^2 \theta}$ Comparing with given equation,  $\tan \theta = 1$  $\Rightarrow \theta = 45^{\circ}$  $\frac{1}{2}g \frac{1}{2} = \frac{2}{2} \Rightarrow u^2 \cos^2 \theta = \frac{25}{2}$ 

$$\frac{1}{2}g\frac{1}{u^2\cos^2\theta} = \frac{1}{5} \Rightarrow u \cos^2\theta = \frac{1}{2}$$
$$\Rightarrow u = 5 \text{ m s}^{-1}$$

11. (d) Vector  $\vec{A}$  is perpendicular to  $\vec{B}$ .

or 
$$(2\hat{i}+3\hat{j}+8\hat{k})\cdot(-4\hat{i}+4\hat{j}+\alpha\hat{k})=0$$
  
-8+12+8 $\alpha$ =0 or  $\alpha$ =-1/2

(c) The angle between velocity and acceleration of a particle describing uniform circular motion is 90°.

**13.** (d) Range, 
$$R = \frac{u^2 \sin 2\theta}{g}$$
 or,  $R \propto \sin 2\theta$ 

Since g is constant and u is same for all the projectiles. So,  $R_A : R_B : R_C = \sin 60^\circ : \sin 90^\circ : \sin 120^\circ$ 

or, 
$$R_A : R_B : R_C = \frac{\sqrt{3}}{2} : 1 : \frac{\sqrt{3}}{2} = \sqrt{3} : 2 : \sqrt{3}$$

 $\therefore R_A = R_C < R_B.$ 

- 14. (a) A vector has a maximum value along its own direction only. Hence the component of a vector  $\vec{r}$  is along positive *x*-axis.
- 15. (c) Given, horizontal range, R = 2H

$$= 2 \times \frac{v^2 \sin^2 \theta}{2g}$$

For maximum height,  $\theta = 90^{\circ}$ 

$$= 2 \times \frac{v^2 \sin^2 90}{2g}$$
$$R = \frac{v^2}{g}$$

16. (c) For the second-hand time period, T = 1 min.

Angular speed 
$$\omega_{\rm s} = \frac{2\pi \text{ rad}}{1 \text{ min}} = \frac{2\pi \text{ rad}}{60 \text{ s}}$$

and that of the hour-hand time period,

$$T = 12 h$$

18.

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Angular speed,

$$\omega_{\rm h} = \frac{2\pi \, \text{rad}}{12 \, \text{h}} = \frac{2\pi \, \text{rad}}{12 \times 60 \times 60 \, \text{s}}$$

Their corresponding ratio is

$$\frac{\omega_{\rm s}}{\omega_{\rm h}} = \frac{\frac{2\pi\,{\rm rad}}{60\,{\rm s}}}{\frac{2\pi\,{\rm rad}}{12\times60\times60\,{\rm s}}} = \frac{12\times60\times60}{60} = \frac{720}{1}$$

**17.** (c) Among the given quantities potential energy is a scalar quantity.

$$(d) \quad H_{max} = \frac{u^2 \sin^2 \theta}{2g}$$

$$\therefore H_{\text{max}} = \frac{(30)^2 \sin^2 45^\circ}{2 \times 10} = \frac{30 \times 30 \times \left(\frac{1}{\sqrt{2}}\right)^2}{2 \times 10}$$
$$= \frac{45}{2} = 22.5 \text{ m}$$



## Limits and Derivatives

1. 
$$\lim_{x \to \frac{\pi}{4}} \frac{\sqrt{2} \cos x - 1}{\cot x - 1}$$
 is equal to [2024]

(a) 2 (b) 
$$\sqrt{2}$$
 (c)  $\frac{1}{2}$  (d)  $\frac{1}{\sqrt{2}}$ 

2. If  $\lim_{x \to 0} \frac{\sin(2+x) - \sin(2-x)}{x} = A \cos B$ , then the values of A and B respectively are [2023] (a) 2, 1 (b) 2, 2 (c) 1, 1 (d) 1, 2

3. If f (x) = 
$$\begin{cases} x^2 - 1, \ 0 < x < 2\\ 2x + 3, \ 2 \le x < 3 \end{cases}$$
, the quadratic equation

whose roots are  $\lim_{x\to 2^{-}} f(x)$  and  $\lim_{x\to 2^{+}} f(x)$  is [2022, 2023] (a)  $x^2 - 14x + 49 = 0$  (b)  $x^2 - 6x + 9 = 0$ 

(c) 
$$x^2-10x + 21 = 0$$
 (d)  $x^2-7x + 8 = 0$ 

4. 
$$\lim_{y \to 0} \frac{\sqrt{3 + y^3} - \sqrt{3}}{y^3} =$$
 [2019, 2022]

(a) 
$$\frac{1}{2\sqrt{3}}$$
 (b)  $2\sqrt{3}$  (c)  $\frac{1}{3\sqrt{2}}$  (d)  $3\sqrt{2}$ 

5. If a and b are fixed non-zero constants, then the derivative of  $\frac{a}{x^4} - \frac{b}{x^2} + \cos x$  is

[2021]

ma + nb - p where

(a) 
$$m = 4x^3$$
;  $n = \frac{-2}{x^3}$ ;  $p = \sin x$   
(b)  $m = \frac{-4}{x^5}$ ;  $n = \frac{2}{x^3}$ ;  $p = \sin x$ 

(c) 
$$m = \frac{-4}{x^5}; n = \frac{2}{x^3}; p = -\sin x$$
  
(d)  $m = 4x^3; n = \frac{2}{x^3}; p = -\sin x$ 

**6.** Consider the following statements:

[2021]

**Statement 1:** 
$$\lim_{x \to 1} \frac{ax^2 + bx + c}{cx^2 + bx + a}$$
 is 1

(where 
$$a + b + c \neq 0$$
)

Statement 2: 
$$\lim_{x \to -2} \frac{\frac{1}{x} + \frac{1}{2}}{x + 2}$$
 is  $\frac{1}{4}$ 

- (a) only statement 2 is true
- (b) only statement 1 is true
- (c) both statements 1 and 2 are true
- (d) both statements 1 and 2 are false

7. The right hand and left hand limit of the function f(x)

$$=\begin{cases} \frac{1}{e^{x}-1}, & \text{if } x \neq 0\\ \frac{1}{e^{x}+1}, & \text{if } x \neq 0 \end{cases} \text{ are respectively} \qquad [2020]\\ 0, & \text{if } x = 0 \end{cases}$$

8. 
$$\lim_{x \to 0} \left( \frac{\tan x}{\sqrt{2x+4}-2} \right)$$
 is equal to [2020]

9. If [x] represents the greatest function and

$$f(x) = x - [x] - \cos x$$
, then  $f'\left(\frac{\pi}{2}\right) =$  [2018]

- (a) 0
  (b) 2
  (c) 1
  (d) does not exist
- **10.** The value of  $\lim_{\theta \to 0} \frac{1 \cos 4\theta}{1 \cos 6\theta}$  is [2017]
  - (a)  $\frac{9}{4}$  (b)  $\frac{4}{9}$  (c)  $\frac{9}{3}$  (d)  $\frac{3}{4}$
- 11.  $\lim_{x \to 0} \frac{xe^x \sin x}{x}$  is equal to [2016]
  - (a) 3 (b) 1 (c) 0 (d) 2
- **12.** If the function g (x) is defined by

#### $g(x) = \frac{x^{200}}{200} + \frac{x^{199}}{199} + \frac{x^{198}}{198} + \dots + \frac{x^2}{2} + x + 5, \text{ then g'(0)}$ is [2015]

(a) 200 (b) 5 (c) 1 (d) 100

14. 
$$\lim_{x \to 0} \frac{1 - \cos x}{x^2}$$
 is [2015]

(a) 3 (b) 
$$1/3$$
 (c) 2 (d)  $\frac{1}{2}$ 

**15.** If the function f(x) satisfies

$$\lim_{x \to 1} \frac{f(x) - 2}{x^2 - 1} = \pi, \text{ then } \lim_{x \to 1} f(x) =$$
 [2014]

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1	(d)	2	(b)	3	(c)	4	(a)	5	(b)	6	(c)	7	(a)	8	(d)	9	(b)	10	(b)
11	(c)	12	(c)	13	(b)	14	(d)	15	(b)										

5



#### Limits and Derivatives

1. (d)  $\lim_{x \to \frac{\pi}{4}} \frac{\sqrt{2}\cos x - 1}{\cot x - 1} = \lim_{x \to \frac{\pi}{4}} \frac{\sqrt{2}\left(\cos x - \frac{1}{\sqrt{2}}\right)\sin x}{\sqrt{2}\left(\frac{1}{\sqrt{2}}\cos x - \frac{1}{\sqrt{2}}\sin x\right)}$ 4.  $= \lim_{x \to \frac{\pi}{4}} \frac{\left(\cos x - \cos \frac{\pi}{4}\right) \sin x}{\sin \frac{\pi}{4} \cdot \cos x - \cos \frac{\pi}{4} \cdot \sin x}$  $= \lim_{x \to \frac{\pi}{4}} \frac{2\sin\left(\frac{x}{2} + \frac{\pi}{8}\right)\sin\left(\frac{\pi}{8} - \frac{x}{2}\right) \cdot \sin x}{\sin\left(\frac{\pi}{4} - x\right)}$ 5  $= \lim_{x \to \frac{\pi}{4}} \frac{2\sin\left(\frac{x}{2} + \frac{\pi}{8}\right) \cdot \sin\left(\frac{\pi}{8} - \frac{x}{2}\right) \cdot \sin x}{2\sin\left(\frac{\pi}{8} - \frac{x}{2}\right) \cdot \cos\left(\frac{\pi}{8} - \frac{x}{2}\right)}$  $= \lim_{x \to \frac{\pi}{4}} \frac{\sin\left(\frac{x}{2} + \frac{\pi}{8}\right) \cdot \sin x}{\cos\left(\frac{\pi}{8} - \frac{x}{2}\right)} = \frac{\sin\frac{\pi}{2} \cdot \sin\frac{\pi}{4}}{\cos^{\circ}} = \frac{1}{\sqrt{2}}$ 6. **(b)**  $\lim_{x \to 0} \frac{\sin(2+x) - \sin(2-x)}{x}$ 2.  $= \lim_{x \to 0} \frac{2\cos(2)\sin(x)}{x}$  $= 2\cos(2)\lim_{x\to 0}\frac{\sin x}{x} = 2\cos(2)$ 7.  $\therefore$  A = 2 & B = 2 (c)  $\lim_{x \to 2^{-}} f(x) = \lim_{h \to 0} f(2-h)$ 3.  $= \lim_{h \to 0} [(2-h)^2 - 1] = 3$  $\lim_{x \to 2^+} f(x) = \lim_{h \to 0} f(2+h) = 2(2+h) + 3 = 7$  $x \rightarrow 2^{+}$ Hence quadratic equation with roots 3 & 7 is  $\Rightarrow$  (x – 3)

$$(x-7)=0$$
  

$$x^{2}-10x+21=0$$
(a)  $\lim_{y\to 0} \frac{\sqrt{3+y^{3}}-\sqrt{3}}{y^{3}}$ 

$$= \lim_{y\to 0} \frac{\left[\frac{(3y^{2})}{2\sqrt{3+y^{3}}}\right]}{3y^{2}} = \frac{1}{2\sqrt{3}}$$
(b)  $y = \frac{a}{x^{4}} - \frac{b}{x^{2}} + \cos x$   
 $\Rightarrow \frac{dy}{dx} = a\left(\frac{-4}{x^{5}}\right) + b\left(\frac{2}{x^{3}}\right) - \sin x$   
 $\Rightarrow ma + nb - p = \left(\frac{-4}{x^{5}}\right)a + \left(\frac{2}{x^{3}}\right)b - \sin x$   
 $m = -\frac{4}{x^{5}}, n = \frac{2}{x^{3}}, p = \sin x$   
(c)  $\lim_{x\to 1} \left(\frac{ax^{2} + bx + c}{cx^{2} + bx + a}\right) = \frac{a + b + c}{c + b + a} = 1.$   
and  $\lim_{x\to 2} \frac{\left(\frac{1}{x} + \frac{1}{2}\right)}{(x+2)} = \frac{1}{4}.$   
(a) RHL =  $\lim_{h\to 0} f(0+h) = \lim_{h\to 0} \frac{e^{\frac{1}{h}} - 1}{e^{\frac{1}{h}} + 1}$   
 $\left(\frac{\infty}{\infty} \text{ form}\right)$ 

$$\Rightarrow \text{RHL} = \lim_{h \to 0} \frac{e^{1/h} \cdot \left(-\frac{1}{h^2}\right)}{e^{1/h} \left(-\frac{1}{h^2}\right)} = 1$$

Now, LHL

$$= \lim_{h \to 0} f(0-h) = \lim_{h \to 0} \left( \frac{e^{-\frac{1}{h}} - 1}{e^{-\frac{1}{h}} + 1} \right) = -1.$$

8. (d) 
$$\lim_{x \to 0} \left( \frac{\tan x}{\sqrt{2x+4}-2} \right)$$

$$= \lim_{x \to 0} \frac{\sec^2 x}{\left(\frac{(2)}{2\sqrt{2x+4}}\right)} = 2$$

**9.** (b)  $f(x) = x - [x] - \cos x$ 

$$f'\left(\frac{\pi}{2}\right) = \lim_{h \to 0} \frac{f\left(\frac{\pi}{2} + h\right) - f\left(\frac{\pi}{2}\right)}{h}$$

$$\left(\frac{\pi}{2} + h\right) - \left[\frac{\pi}{2} + h\right] - \cos\left(\frac{\pi}{2} + h\right) - \left[\frac{\pi}{2} + h\right] - \cos\left(\frac{\pi}{2} + h\right) - \left[\frac{\pi}{2}\right] + \cos\left(\frac{\pi}{2}\right) + \left[\frac{\pi}{2}\right] + \cos\left(\frac{\pi}{2}\right) + \left[\frac{\pi}{2}\right] + \cos\left(\frac{\pi}{2}\right) + \left[\frac{\pi}{2}\right] + \cos\left(\frac{\pi}{2} + h\right) + 1$$

$$= \lim_{h \to 0} \frac{h - 1 - \cos\left(\frac{\pi}{2} + h\right) + 1}{h}$$

$$\left\{ \because \left[\frac{\pi}{2}\right] = \lim_{h \to 0} \left[\frac{\pi}{2} + h\right] = 1 \right\}$$

$$= \lim_{h \to 0} \frac{1 + \sin\left(\frac{\pi}{2} + h\right)}{1} = 2$$

10. (b) 
$$\lim_{\theta \to 0^{\circ}} \frac{1 - \cos 4\theta}{1 - \cos 6\theta} = \lim_{\theta \to 0^{\circ}} \frac{\sin 4\theta \cdot (4)}{\sin 6\theta \cdot (6)}$$
$$= \lim_{\theta \to 0} \frac{\cos 4\theta (16)}{\cos 6\theta (36)} = \frac{4}{9}$$
  
11. (c) 
$$\lim_{x \to 0} \frac{xe^{x} - \sin x}{x} = \lim_{x \to 0} \frac{(xe^{x} + e^{x} - \cos x)}{(1)}$$
$$= 0$$
  
12. (c) 
$$g(x) = \frac{x^{200}}{200} + \frac{x^{199}}{199} + \frac{x^{198}}{198} + \frac{x^{198}}{198} + \frac{x^{199}}{199} + \frac{x^{198}}{198} + \frac{x^{198}}{198} + \frac{x^{199}}{199} + \frac{x^{198}}{198} + \frac{x^{199}}{199} + \frac{x^{198}}{198} + \frac{x^{199}}{199} + \frac{x^{198}}{198} + \frac{x^{198}}{198} + \frac{x^{198}}{198} + \frac{x^{199}}{199} + \frac{x^{198}}{198} + \frac{x^{199}}{199} + \frac{x^{198}}{198} + \frac{x^{198}}{198} + \frac{x^{198}}{198} + \frac{x^{198}}{198} + \frac{x^{198}}{198} + \frac{x^{199}}{198} + \frac{x^{198}}{198} + \frac{x^{$$

 $\Rightarrow \lim_{x \to 1} f(x) - 2 = \pi(0) \Rightarrow \lim_{x \to 1} f(x) = 2$